

## Section Handout #6

---

### Problem 1: Rationals and Unit Fractions

For this problem, you may assume the `Rational` class we implemented in lecture has been extended to provide `getNumerator` and `getDenominator` methods. Implement a function called `unitFractionSum`, which accepts a `Rational` object called `r`—assumed to be between 0 and 1—and returns a list of strictly decreasing unit fractions—that is, fractions with a numerator of 1—whose sum is `r`. If `r` is already a unit fraction, then `unitFractionSum` should just return the list `[r]`. Otherwise, compute the largest unit fraction—we'll call it `u`—that's less than `r` and add `u` to a running list of unit fractions that eventually add up to `r`. It's an iterative process where you're always computing the largest unit fraction less than or equal to what's left.

```
def unitFractionSum(r):
    """
    Constructs a list of distinct unit fraction
    that add up to the supplied r.
    Examples:
        unitFractionSum(Rational(1, 3)) -> [1/3]
        unitFractionSum(Rational(2, 3)) -> [1/2, 1/6]
        unitFractionSum(Rational(21, 23)) -> [1/2, 1/3, 1/13, 1/359, 1/644046]
    """
```

Now extend the above function to generate a sum of unit fractions (with minimum denominator of 2) for any positive rational number whatsoever, ensuring that no denominator gets used more than once.

```
def unitFractionSum(r):
    """
    Constructs a list of distinct unit fraction
    that add up to the supplied r.
    Examples:
        unitFractionSum(Rational(21, 23)) -> [1/2, 1/3, 1/13, 1/359, 1/644046]
        unitFractionSum(Rational(13, 12)) -> [1/2, 1/3, 1/4]
        unitFractionSum(Rational(5, 2)) ->
            [1/2, 1/3, ..17 terms.. ,1/7894115294, 1/333156570077494116352]
    """
```



For this problem, you're to provide the full implementation of the `PresidentialWordCloud` class, whose constructor accepts the name of a valid, properly structured file and makes a single pass through it to build an internal representation of the relevant data and configure the object so it responds to two methods, which are:

- `getAllWords`, which accepts `title` and `date` strings as arguments and returns the alphabetically sorted list of words that would contribute to that speech's word cloud, and
- `getAllTags`, which accepts `title`, `date`, and `size` parameters and returns a list of Python tuples, alphabetically sorted by word, for all tagged words in the speech identified by the supplied title and date that should be rendered in the supplied font size. Each tuple should be of length two: the 0<sup>th</sup> entry should be the word and the 1<sup>th</sup> entry should be the color. For example, a call to `cloud.getAllTags("Foundation of Government", "1776-01-15", 15)` would produce the following list as a return value:

```
[
    ("affections", "#A19A7E"), ("agreeable", "#BBB6A2"),
    ("ambition", "#D9D6CB"), ("antiquity", "#8C8361"),
    // several similarly structured tuples omitted for brevity
    ("youth", "#DEDCD2")
]
```

The two methods shouldn't need to do anything other than quickly lookup and return information stored in dictionaries fully built by the constructor. Whenever the speech/date and speech/date/size combinations can't be found, you should return the empty list.